

The other three quotients contain a loop and contribute zero under the loopless contract.

$$H = I + e \quad \Longrightarrow \quad \widehat{H} - \widehat{I} - \widehat{e} \neq 0 \;\Rightarrow\; \text{no common realizing target}$$